

**Zadatak 1.1. Sabrati sadržaj dva 16-bitna registra kao celobrojne vrednosti.**

**Registar 1**

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	0	0	0	0	0	1	1	1	0	1	0	1	0

**Registar 2**

0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**

$$(2^7 + 2^6 + 2^5 + 2^3 + 2^1) + (2^3 + 2^2 + 2^1 + 2^0) = 234 + 15 = 249$$

**Zadatak 1.2. Sabrati sadržaj dva 16-bitna registra kao celobrojne vrednosti.**

**Registar 1**

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	1	0	0	1	0	0	0	1	1	1	0	1	0	0	0

**Registar 2**

0	1	0	1	1	0	0	0	1	0	0	0	1	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**

$$(-2^{15} + 2^{14} + 2^{11} + 2^7 + 2^6 + 2^5 + 2^3) + (2^{14} + 2^{12} + 2^{11} + 2^7 + 2^3 + 2^2) = -14104 + 22668 = 8564$$

**Zadatak 2.1. Sabrati sadržaj dva 16-bitna registra kao razlomačke vrednosti.**

**Registar 1**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	0	0	1	1	1	0	1	0	1	0

**Registar 2**

0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**  $(2^{-8} + 2^{-9} + 2^{-10} + 2^{-12} + 2^{-14}) + (2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}) =$   
 $0,00714111328125 + 0,000457763671875 = 0,007598876953125$

**Zadatak 2.2. Sabrati sadržaj dva 16-bitna registra kao razlomačke vrednosti.**

**Registar 1**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	0	0	1	0	0	0	1	1	1	0	1	0	0	0

**Registar 2**

0	1	0	1	1	0	0	0	1	0	0	0	1	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**

$(-2^0 + 2^{-1} + 2^{-4} + 2^{-8} + 2^{-9} + 2^{-10} + 2^{-12}) + (2^{-1} + 2^{-3} + 2^{-4} + 2^{-8} + 2^{-12} + 2^{-13}) =$   
 $-0,430419921875 + 0,6917724609375 = 0,2613525390625$

**Zadatak 2.3. Sabrati sadržaj dva 16-bitna registra kao razlomačke vrednosti u formatu <s.2.13>**

**Registar 1**

2	1	0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	1	0	0	1	0	0	0	1	1	1	0	1	0	0	0

**Registar 2**

0	1	0	1	1	0	0	0	1	0	0	0	1	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**

$$(-2^2 + 2^1 + 2^{-2} + 2^{-6} + 2^{-7} + 2^{-8} + 2^{-10}) + (2^1 + 2^{-1} + 2^{-2} + 2^{-6} + 2^{-10} + 2^{-11}) =$$

$$-1,7216796875 + 2,76708984375 = 1,04541015625$$

**Zadatak 2.4. Prikazati sadržaj registara sabiraka i zbiru u binarnom sistemu ako su sabirci „4.51“ i „-6.32“**

**Rešenje:**

Broj 8 ili  $2^3$  je prvi stepen broja dva koji je veći od maksimuma apsolutnih vrednosti ova dva sabirka, stoga će nam biti potreban format <s.3.12>, 3 bita za celi deo broja i 12 za razlomljeni.

$$4 = 2^2$$

$$0.51 = 2^{-1} + 2^{-7} + 2^{-9}$$

$$4.51 =$$

3	2	1	0	1	2	3	4	5	6	7	8	9	10	11	12
0	1	0	0	1	0	0	0	0	0	1	0	1	0	0	0

$$6 = 2^2 + 2^1$$

$$0.32 = 2^{-2} + 2^{-4} + 2^{-8} + 2^{-9} + 2^{-10} + 2^{-11}$$

Da bi drugi sabirak predstavili kao negativan broj, potrebno je jos uraditi drugi koplement broja 2 (invertovanje svih bita i sabiranje sa "1").

$$6.32 =$$

3	2	1	0	1	2	3	4	5	6	7	8	9	10	11	12
0	1	1	0	0	1	0	1	0	0	0	1	1	1	1	0

$$\text{Invertujemo} =$$

1	0	0	1	1	0	1	0	1	1	1	0	0	0	0	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

$$+$$

															1
--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	---

$$-6.32 =$$

1	0	0	1	1	0	1	0	1	1	1	0	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

I na kraju treba jos zbir izračunati:

$$4,509765625 = \begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|} \hline 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 \\ \hline \end{array}$$

+

$$-6.31982421875 = \begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|} \hline 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ \hline \end{array}$$

$$-1.81005859375 = \begin{array}{|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|c|} \hline 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ \hline \end{array}$$

$$(2^2 + 2^{-1} + 2^{-7} + 2^{-9}) + (-2^3 + 2^0 + 2^{-1} + 2^{-3} + 2^{-5} + 2^{-6} + 2^{-7} + 2^{-11}) =$$

$$4,509765625 - 6,31982421875 = -1,81005859375$$

**Zadatak 3.1. Pomnožiti sadržaje dva 16-bitna registra kao razlomačke vrednosti u formatu <s.0.15>**

**Registar 1**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	0	0	1	0	0	0	1	1	1	0	1	0	0	0

**Registar 2**

0	1	0	1	1	0	0	0	1	0	0	0	1	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**Rešenje:**

$$\langle s.0.15 \rangle * \langle s.0.15 \rangle = \langle s. (0 + 0) . (15 + 15 + 1) \rangle = \langle s.0.31 \rangle$$

$$(-2^0 + 2^{-1} + 2^{-4} + 2^{-8} + 2^{-9} + 2^{-10} + 2^{-12}) * (2^{-1} + 2^{-3} + 2^{-4} + 2^{-8} + 2^{-12} + 2^{-13}) =$$

$$= -0,430419921875 * 0,6917724609375 = -0,2977526485919952392578125$$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	0	1	1	0	0	1	1	1	1	0	0	0	1	1
16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
0	0	1	1	1	1	0	1	1	1	0	0	0	0	0	0

**Zadatak 3.2.** Pomnožiti sadržaje dva 16-bitna registra kao razlomačke vrednosti ako je format prvog množioca <s.3.12> a drugog <s.7.8>

3	2	1	0	1	2	3	4	5	6	7	8	9	10	11	12
1	0	0	0	1	0	0	0	1	0	1	0	1	0	0	0

**Registar 2**

7	6	5	4	3	2	1	0	1	2	3	4	5	6	7	8
0	1	0	1	0	0	0	0	0	0	0	0	1	1	0	0

**Rešenje:**

$$\begin{aligned} \langle s.3.12 \rangle * \langle s.7.8 \rangle &= \langle s. (3 + 7) \cdot (12 + 8 + 1) = \langle s.10.21 \rangle \\ (-2^3 + 2^{-1} + 2^{-5} + 2^{-7} + 2^{-9}) * (2^6 + 2^4 + 2^{-5} + 2^{-6}) &= -7,458984375 * 80,046875 = \\ -597,068389892578125 \end{aligned}$$

10	9	8	7	6	5	4	3	2	1	0	1	2	3	4	5
1	0	1	1	0	1	0	1	0	1	0	1	1	1	0	1

6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
1	1	0	0	1	1	1	1	1	1	0	0	0	0	0	0

**Zadatak 3.3.** Pomnožiti sadržaje dva 16-bitna registra kao razlomačke vrednosti ako je format prvog množioca <s.1.14> a drugog <s.3.12>, a zatim njihov proizvod sabrati sa vrednošću trećeg registra čiji je format <s.5.10>.

**Registar 1**

1	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	1	0	0	0	1	0	1	0	1	0	0	0

**Registar 2**

3	2	1	0	1	2	3	4	5	6	7	8	9	10	11	12
0	1	0	1	0	0	0	0	0	0	0	0	1	1	0	0

**Registar 3**

5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	10
0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0

## Rešenje:

Množenje prva dva registra:

$$(2^{-3} + 2^{-7} + 2^{-9} + 2^{-11}) * (2^2 + 2^0 + 2^{-9} + 2^{-10}) = 0,13525390625 * 5,0029296875 =$$

0,676665782928466796875

$$\langle \text{s.1.14} \rangle * \langle \text{s.3.12} \rangle = \langle \text{s.} (1 + 3) \cdot (14 + 12 + 1) = \langle \text{s.4.27} \rangle$$

4	3	2	1	0	1	2	3	4	5	6	7	8	9	10	11
0	0	0	0	0	1	0	1	0	1	1	0	1	0	0	1
12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	1	0	0	1	1	1	1	1	1	1	0	0	0	0	0

Sabirci u aritmetici fiksnog zareza moraju biti u istom formatu za razliku od mnozioca. Postoje dve mogućnosti da se izravnaju formati ili da se sabirak iz trećeg registra pomeri za jedno mesto u levo ili da se proizvod pomeri za jedno mesto u desno. U ovom slučaju proizvod konvertujemo u format  $\langle \text{s.5.10} \rangle$  pomeranjem sadržaja registra za jedno mesto u desno. Na mesto bita sa najvisom tezinom se postavlja ulazna nula jer je broj pozitivan.

Posle pomeranja proizvod izgleda ovako:

5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	1	0	1	0	1	1	0	1	0
11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	1	1	0	0	1	1	1	1	1	1	1	0	0	0

+

5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	10
0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0

Sabiraju se biti istih težina, tj gornjih 16 bita proizvoda i sabirak trećeg registra., posle sabiranja rezultat je:

5	4	3	2	1	0	1	2	3	4	5	6	7	8	9	10
0	0	0	1	0	0	0	1	0	1	1	0	1	0	1	0
11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	1	1	0	0	1	1	1	1	1	1	0	0	0	0